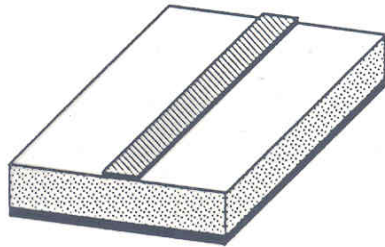


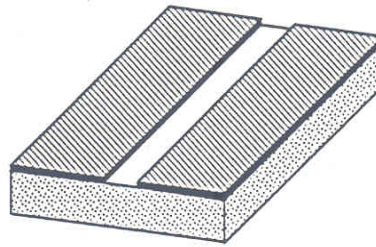
Printed lines

- microstrip lines
- slot lines
- striplines
- coplanar waveguides

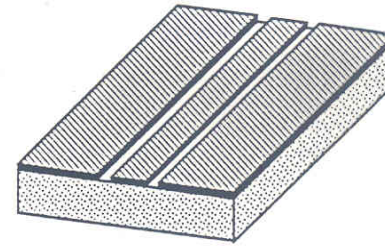
Printed lines



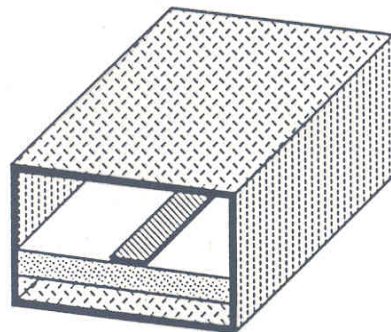
Microstrip



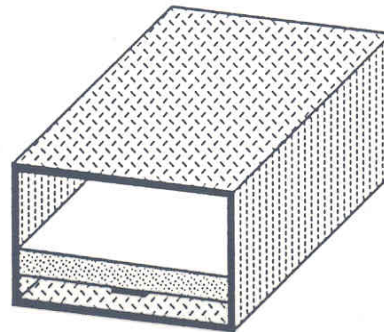
Slotline



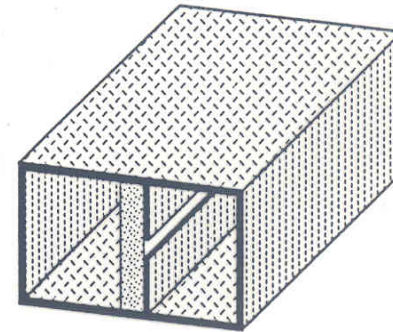
Coplanar Line



Suspended Stripline

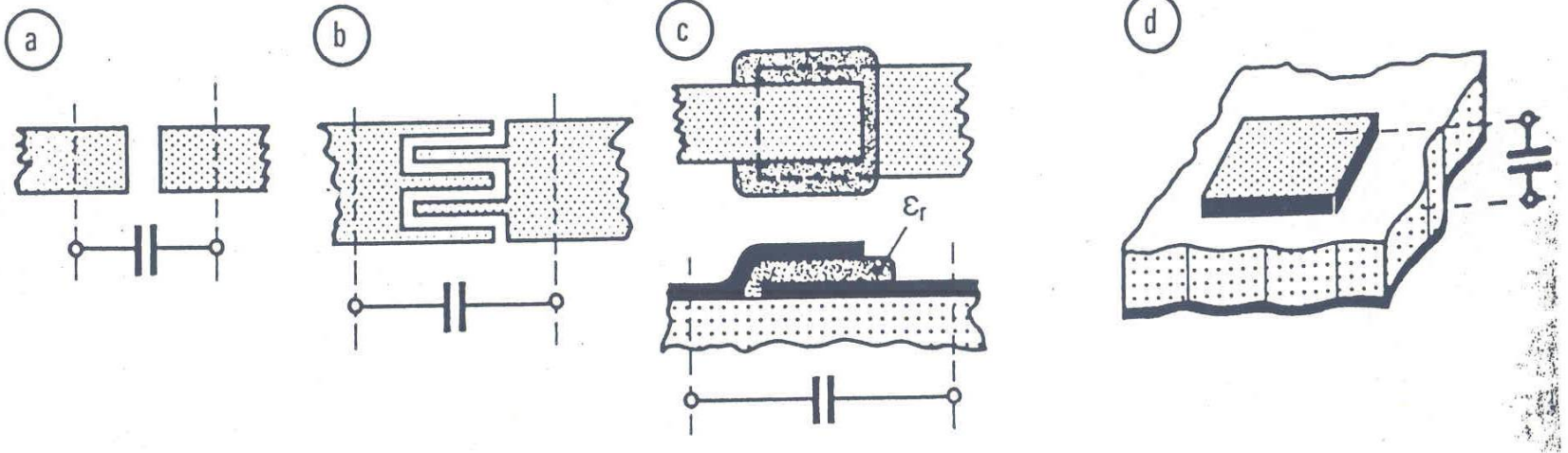


Inverted Stripline

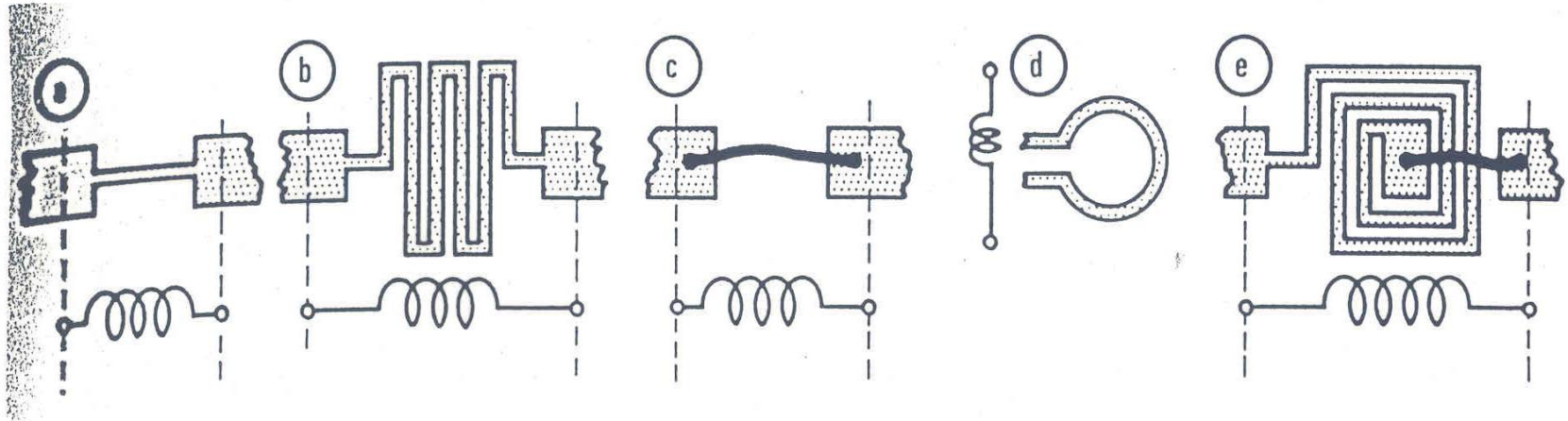


Fin Line

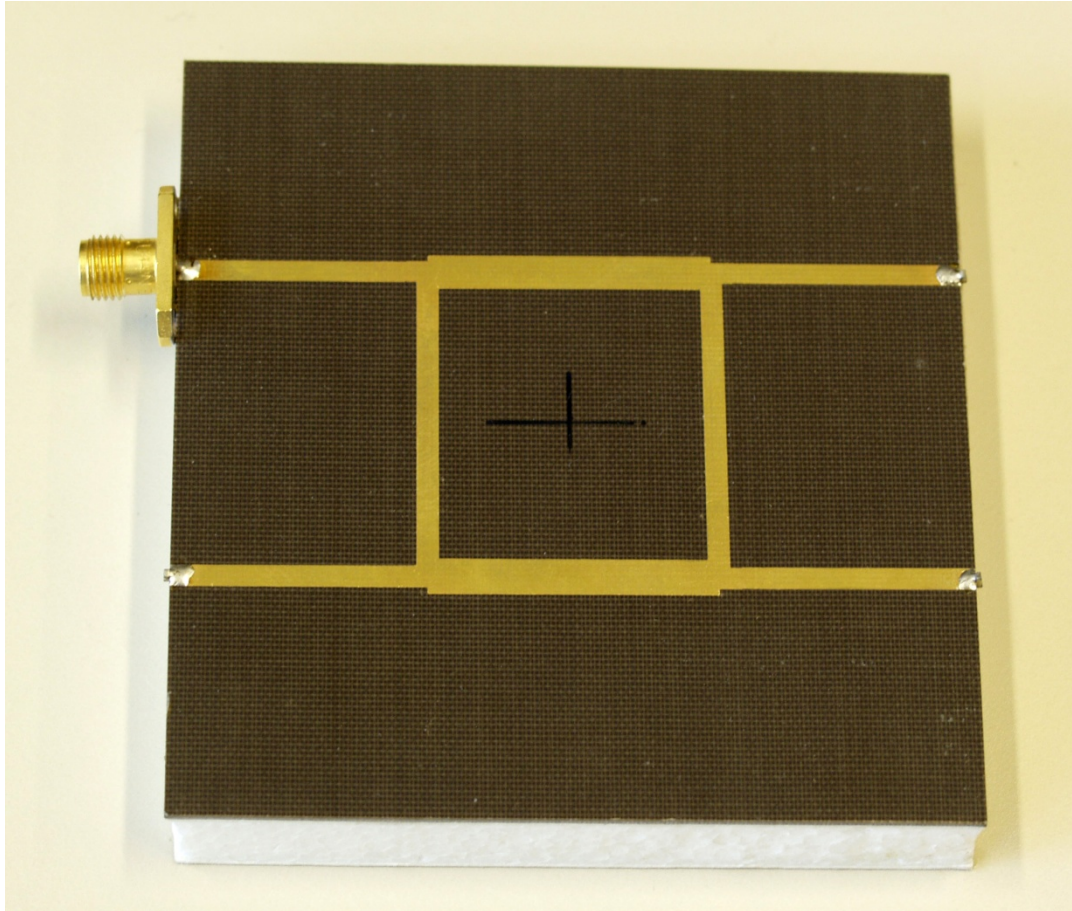
Printed lines

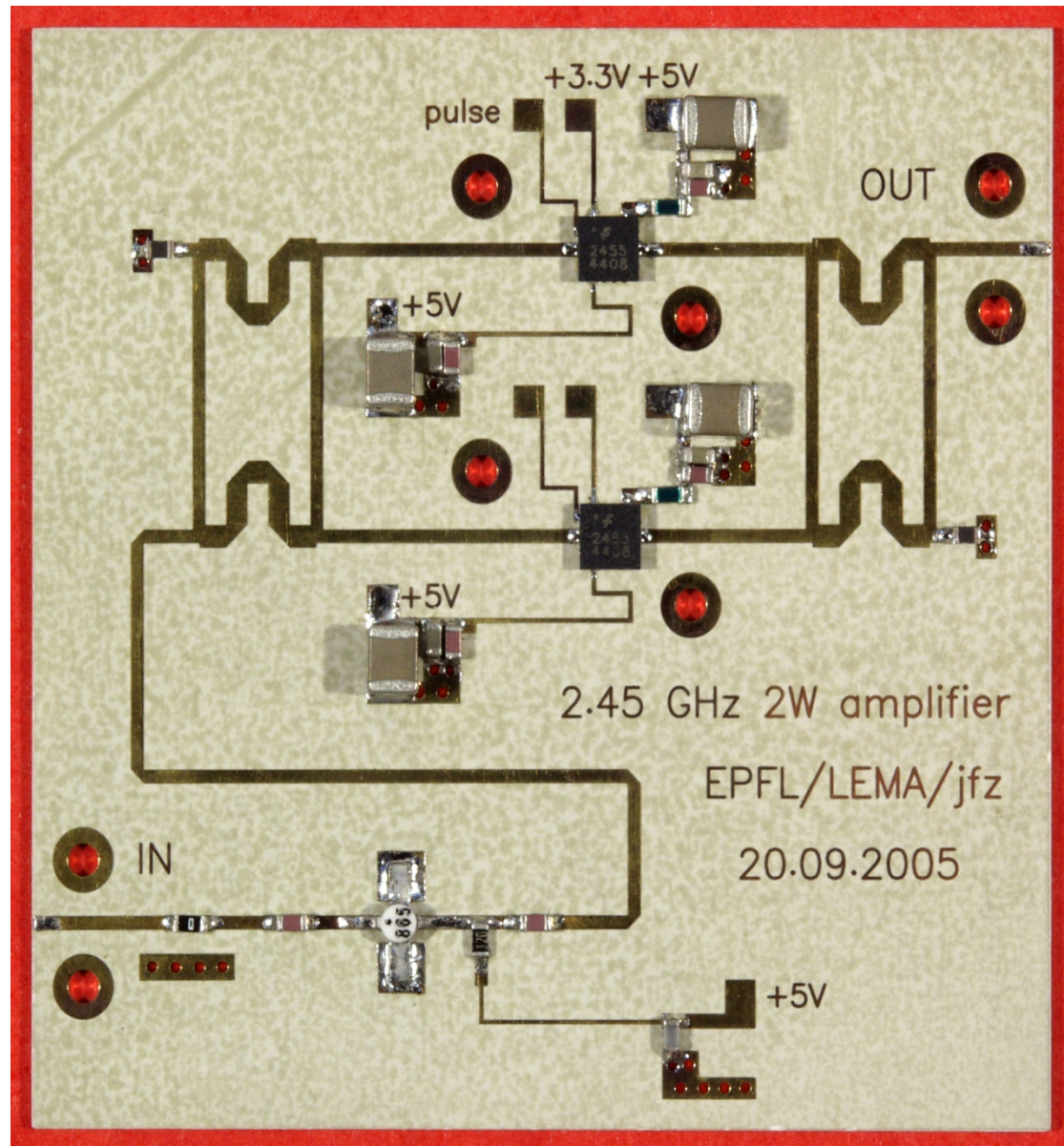


Printed lines

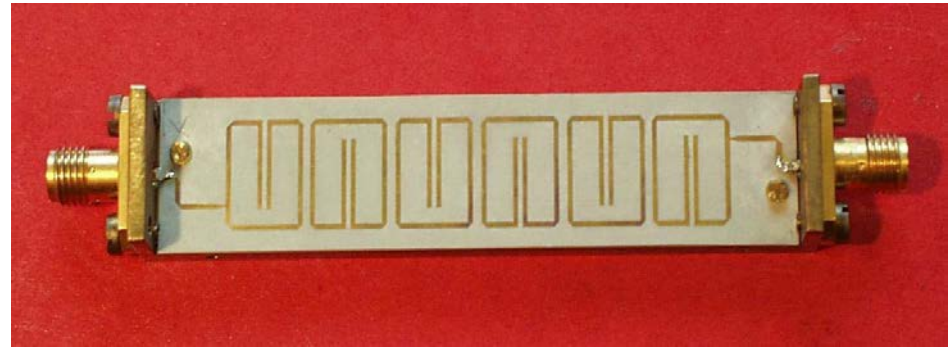
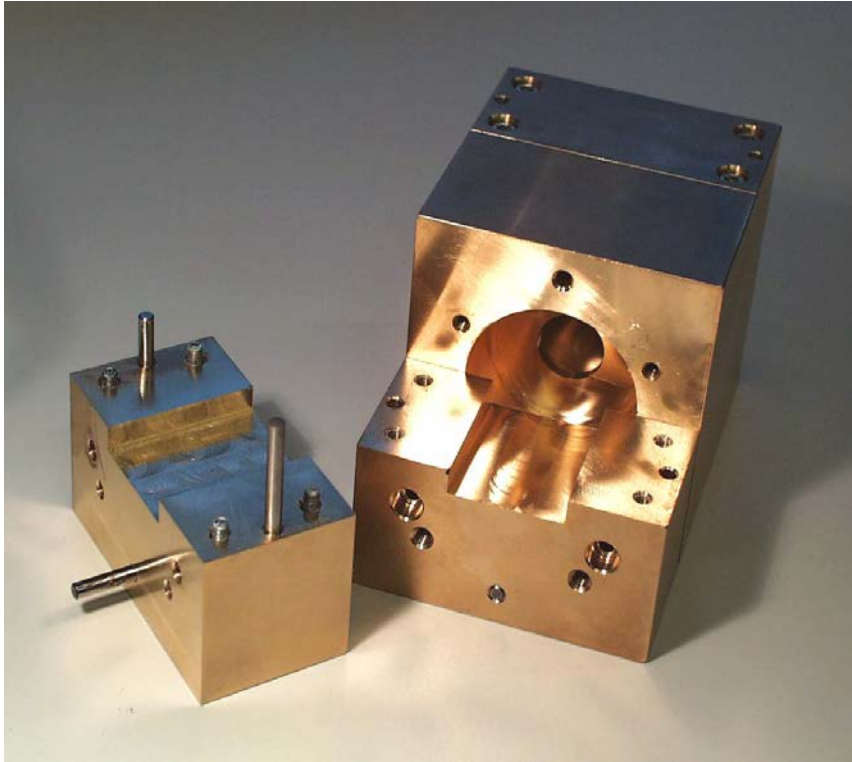


Printed lines

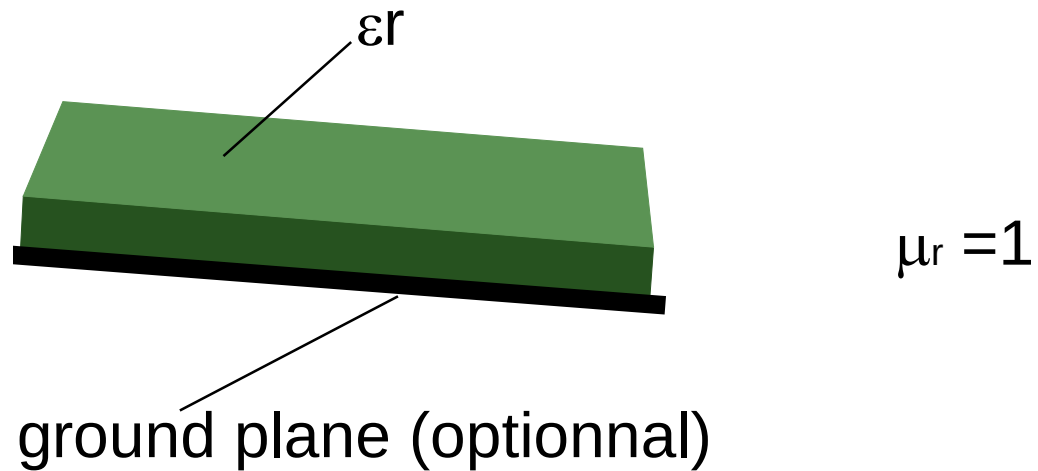




Printed lines



Dielectric substrate



Usual substrates : ceramics

- Ceramics : Alumina (Al_2O_3) and Beryllium Oxides (BeO)
 - $6 < \epsilon_r < 10$ $2 \cdot 10^{-4} < \tan \delta < 4 \cdot 10^{-4}$
- Synthetic materials

Usual substrates : synthetic materials

- Polystyren, polyolfin, polyester, polytetrafluoretylen (Teflon)
 - $2 < \epsilon_r < 3$ $\tan \delta$ around $5 \cdot 10^{-4}$
- Synthetic materials charged with ceramic powder or glass fibres
 - $2 < \epsilon_r < 10$ $\tan \delta$ around $1 \cdot 10^{-3}$
- FR4
 - $\epsilon_r = 4.4$ $\tan \delta$ around $2 \cdot 10^{-2}$

EPFL Usual substrates : integrated circuit substrates

- Silicon

$$\epsilon_r = 11.9 \quad \tan \delta \text{ around } 4 \cdot 10^{-4}$$

- Gallium Arsenide

$$\epsilon_r = 13 \quad \tan \delta \text{ around } 6 \cdot 10^{-4}$$

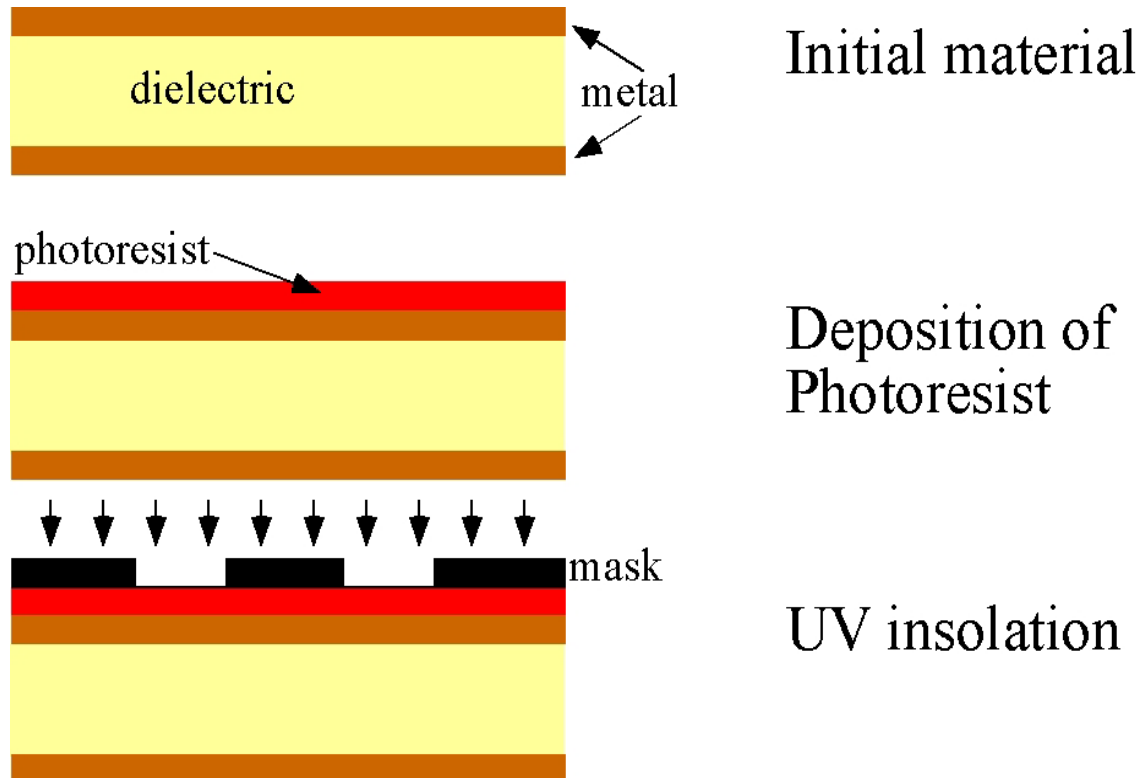
Printed microwave lines : advantages

- Cheap
- easy to manufacture
- good repetability
- Light in weight, lowprofile
- Compatible with integrated circuits

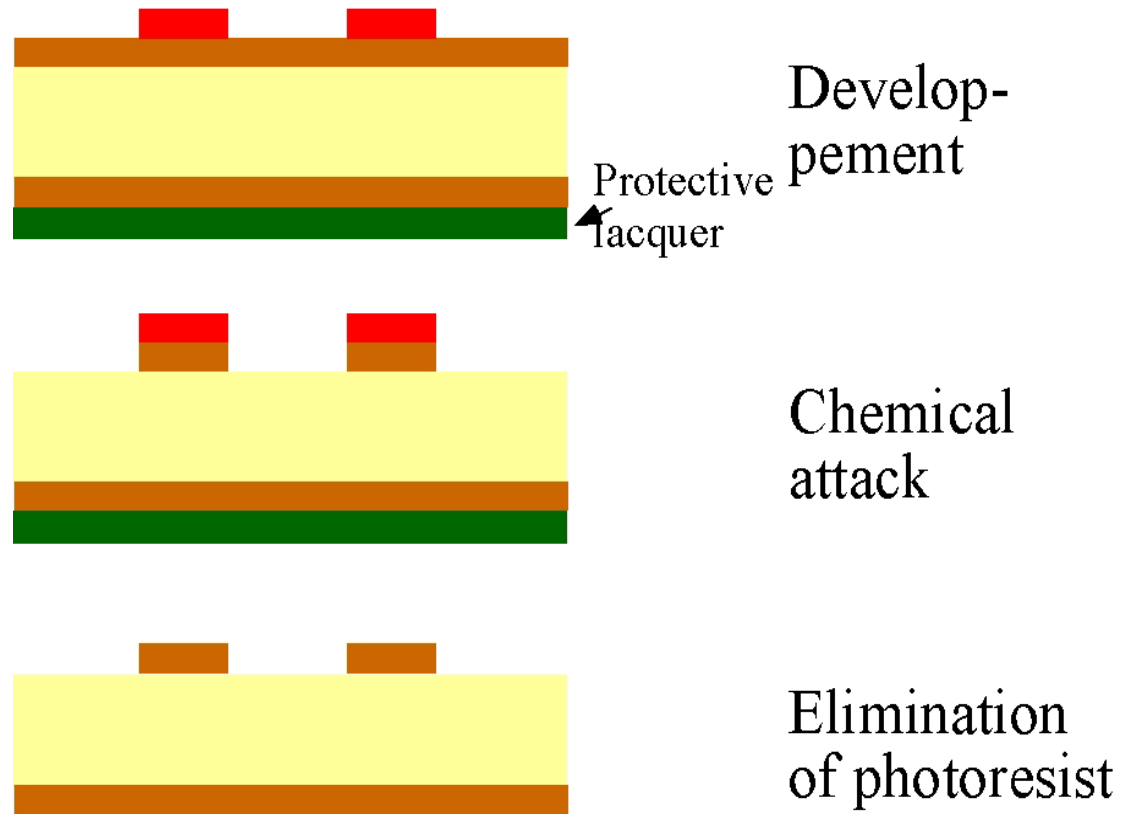
Printed microwave lines : drawbacks

- relative high losses
- dispersion
- inhomogeneous structures , thus difficult to analyze

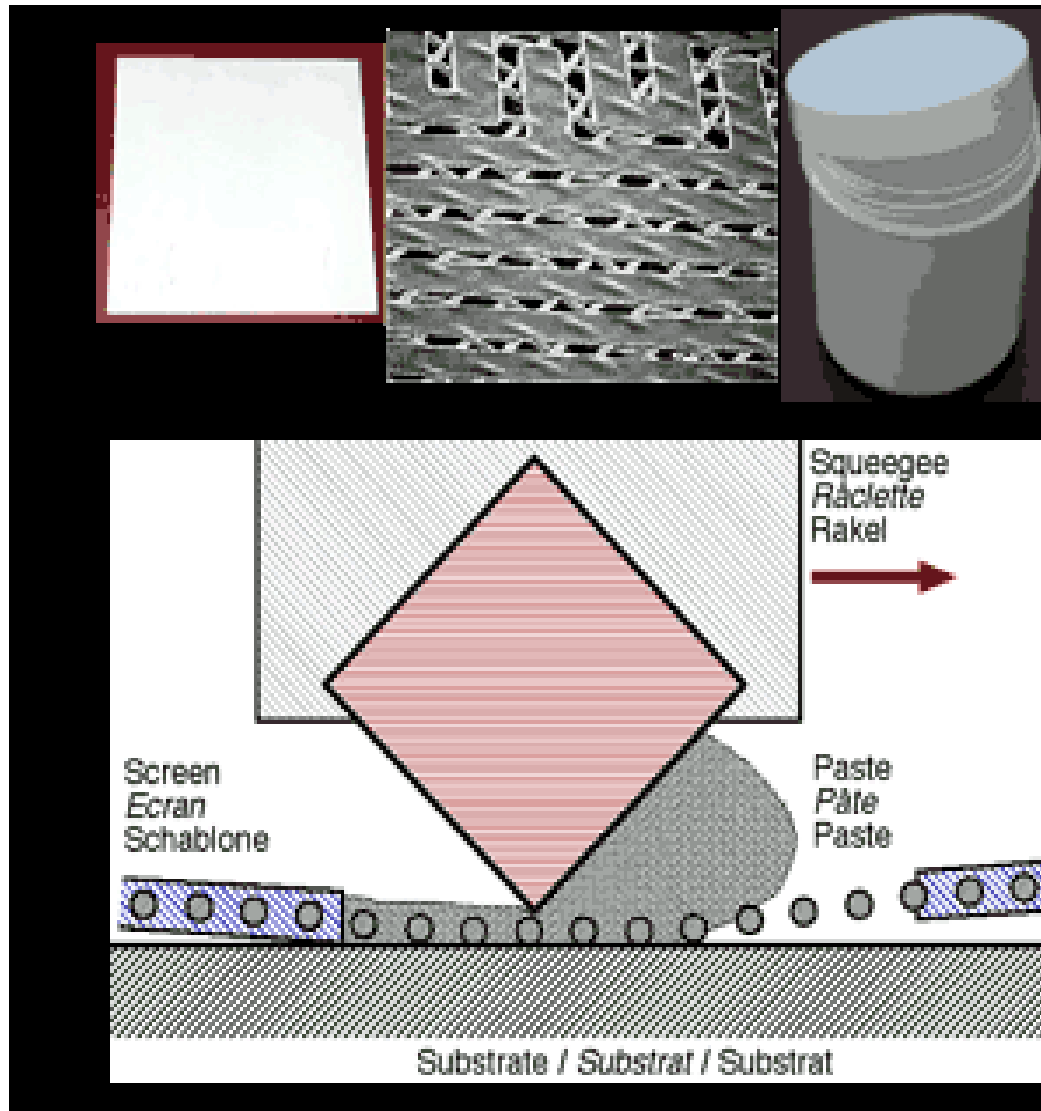
Thinn film manufacturing process



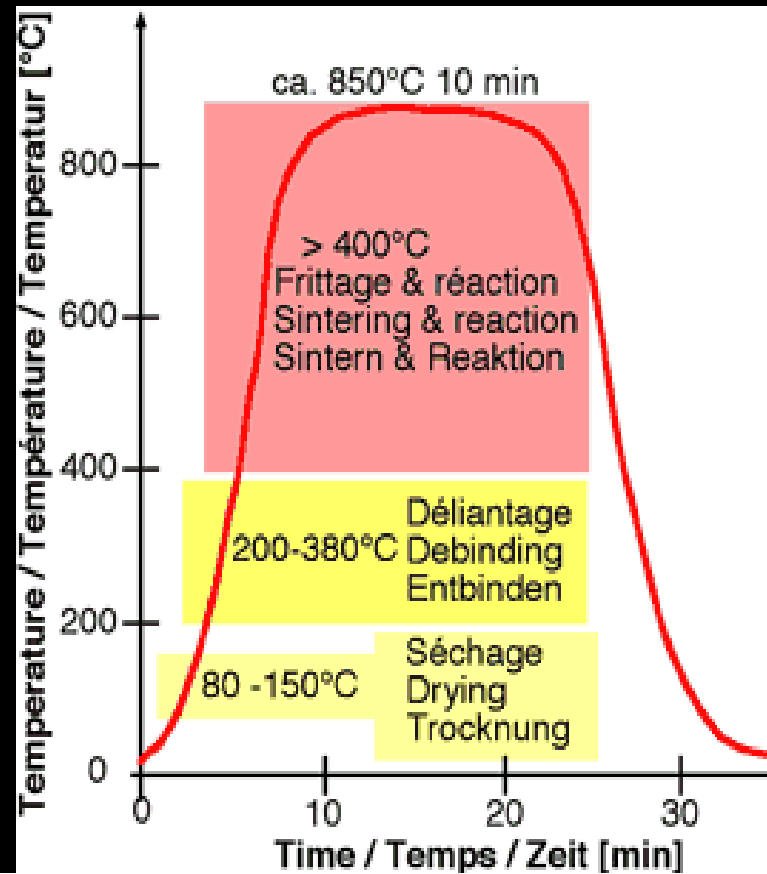
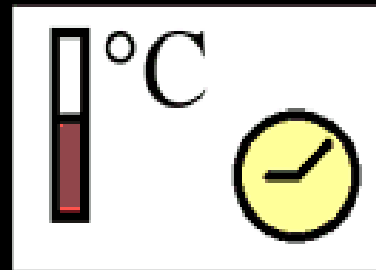
Thinn film manufacturing process



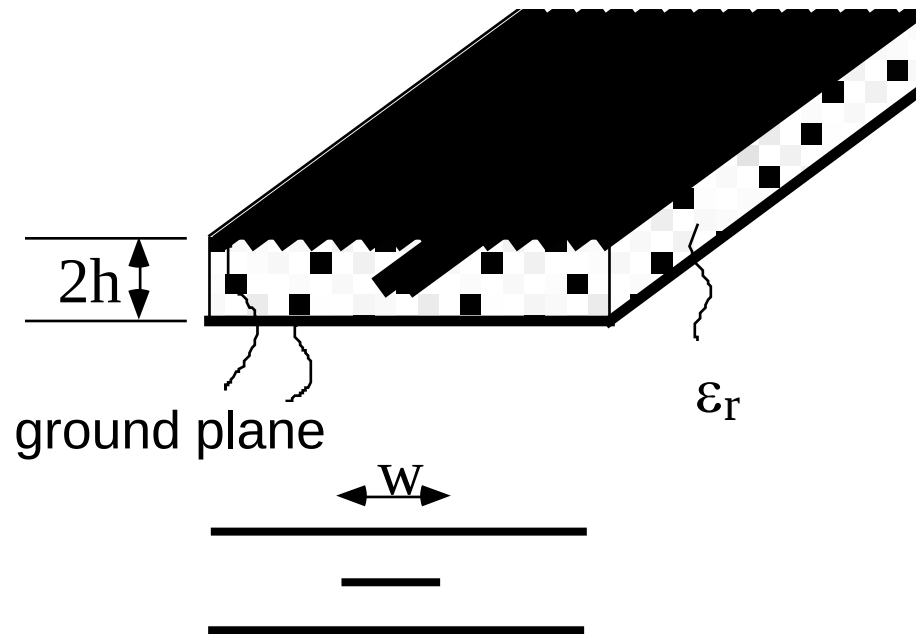
Thick film



Thick film



Stripline



stripline

- homogeneous dielectric
- two distinct conductors

TEM mode is supported

stripline : TEM modes

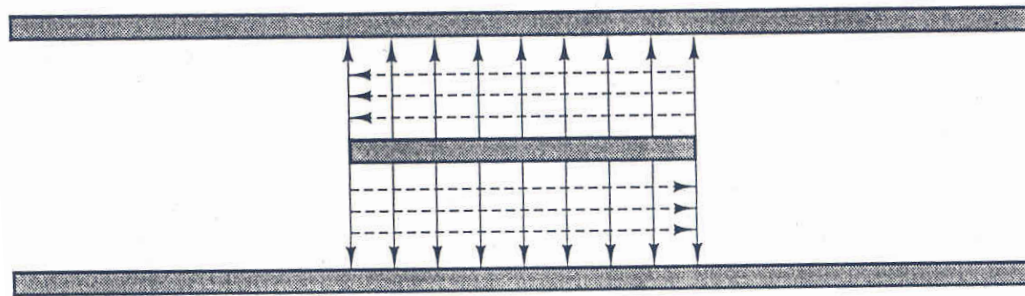
- We want to know :
 - Characteristic impedance
 - group velocity
 - phase velocity
 - propagation constant
 - guided wavelength

Stripline : approximation

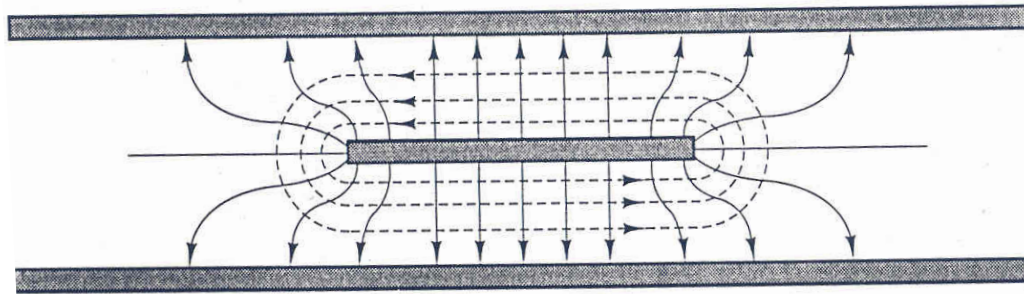


Stripline equivalent to two parallel plate waveguides in parallel

Stripline : approximation

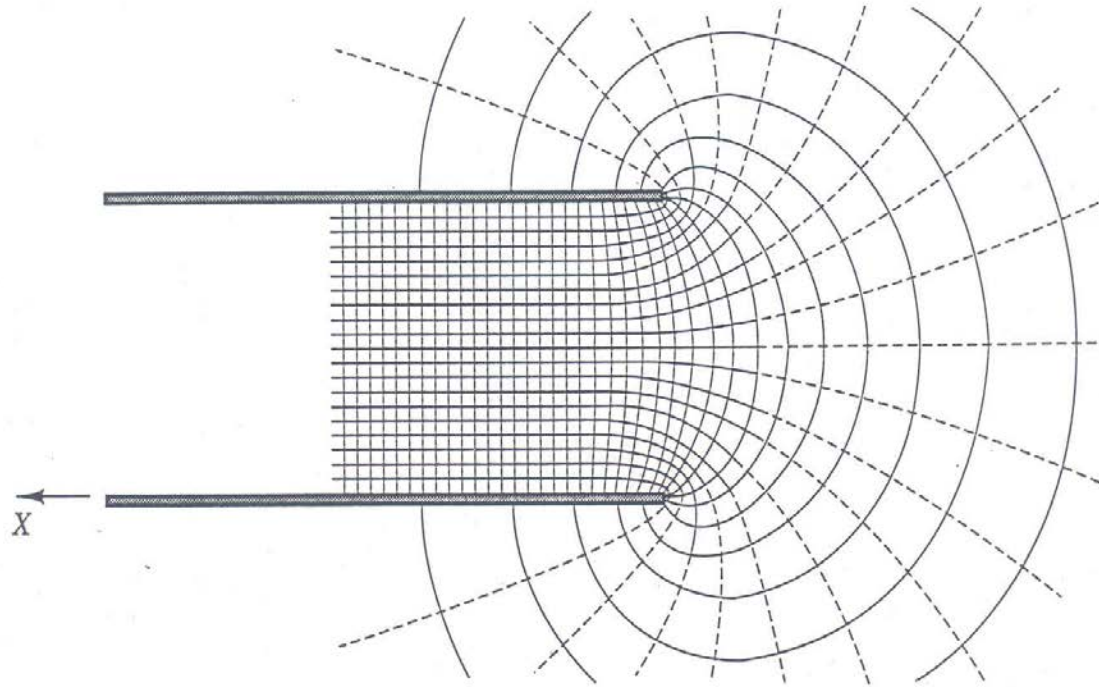


(b)

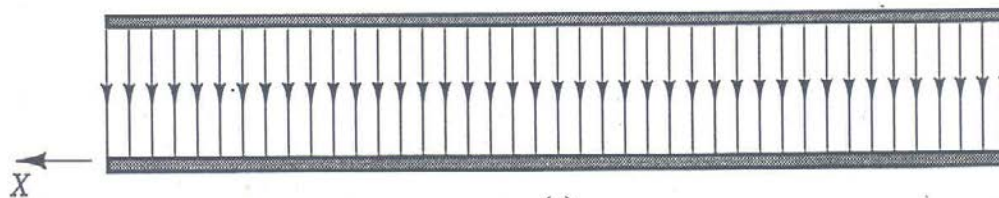


(d)

Parallel plate waveguide



(b)



(c)

Parallel plate waveguide : TEM mode

$$\beta = \omega \sqrt{\epsilon_r \epsilon_0 \mu_0} = \sqrt{\epsilon_r} k_0$$

$$v_\phi = \frac{\omega}{\beta} = \frac{1}{\sqrt{\epsilon_r \epsilon_0 \mu_0}} = \frac{c}{\sqrt{\epsilon_r}}$$

$$v_g = \left(\frac{\partial \beta}{\partial \omega} \right)^{-1} = \frac{1}{\sqrt{\epsilon_r \epsilon_0 \mu_0}} = \frac{c}{\sqrt{\epsilon_r}}$$

$$\lambda = \frac{2\pi v_\phi}{\omega} = \frac{\lambda_0}{\sqrt{\epsilon_r}}$$

Parallel plate waveguide : TEM mode

Characteristic impedance

$$u(z) = - \int_{y=0}^{y=b} \mathbf{E} \cdot d\mathbf{l} = V_o e^{-\gamma z}$$

$$i(z) = \oint_{\text{1conduct}} \mathbf{H} \cdot d\mathbf{l} = \frac{\sqrt{\epsilon_r \epsilon_o} V_o}{\sqrt{\mu_o}} \frac{w}{b} e^{-\gamma z}$$

$$Z_o = 120 \pi$$

$$Z_c = \frac{u}{i} = \frac{b}{w} \frac{\sqrt{\mu_o}}{\sqrt{\epsilon_r \epsilon_o}} = \frac{b}{w} \frac{Z_o}{\sqrt{\epsilon_r}}$$

Stripline

Propagation coeff., phase and group velocities,
wavelength identical to parallel plate waveguide

$$\beta = \omega \sqrt{\epsilon_r \epsilon_0 \mu_0} = \sqrt{\epsilon_r} k_0$$

$$v_\phi = \frac{\omega}{\beta} = \frac{1}{\sqrt{\epsilon_r \epsilon_0 \mu_0}} = \frac{c}{\sqrt{\epsilon_r}}$$

$$v_g = \left(\frac{\partial \beta}{\partial \omega} \right)^{-1} = \frac{1}{\sqrt{\epsilon_r \epsilon_0 \mu_0}} = \frac{c}{\sqrt{\epsilon_r}}$$

$$\lambda = \frac{2\pi v_\phi}{\omega} = \frac{\lambda_0}{\sqrt{\epsilon_r}}$$

Stripline

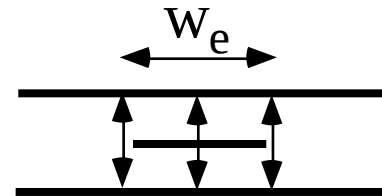
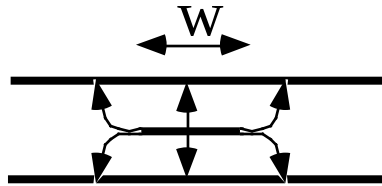
Characteristic impedance corresponding in first approximation to two parallel plate waveguides in parallel

$$Z_c = \left(\frac{1}{Z_c^{paral.}} + \frac{1}{Z_c^{paral.}} \right)^{-1} = \frac{h}{2w} \frac{Z_o}{\sqrt{\epsilon_r}}$$

Stripline : second order approximation (analysis)

$$Z_c = \frac{30\pi}{\sqrt{\epsilon_r}} \frac{2h}{w_e + 0.441(2h)}$$

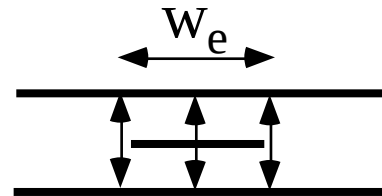
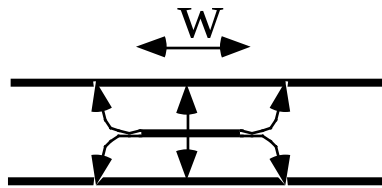
$$\frac{w_e}{2h} = \frac{w}{2h} - \begin{cases} 0 & \text{pour } \frac{w}{2h} > 0.35 \\ \left(0.35 - \frac{w}{2h}\right)^2 & \text{pour } \frac{w}{2h} < 0.35 \end{cases}$$



Stripline : second order approximation (synthesis)

$$\frac{w}{2h} = \begin{cases} x & \text{pour } \sqrt{\epsilon_r} Z_c < 120 \\ 0.85 - \sqrt{0.6 - x} & \text{pour } \sqrt{\epsilon_r} Z_c > 120 \end{cases}$$

$$x = \frac{30\pi}{\sqrt{\epsilon_r} Z_c} - 0.441$$



Stripline : attenuation

$$\alpha = \alpha_d + \alpha_c \quad [Np/m]$$

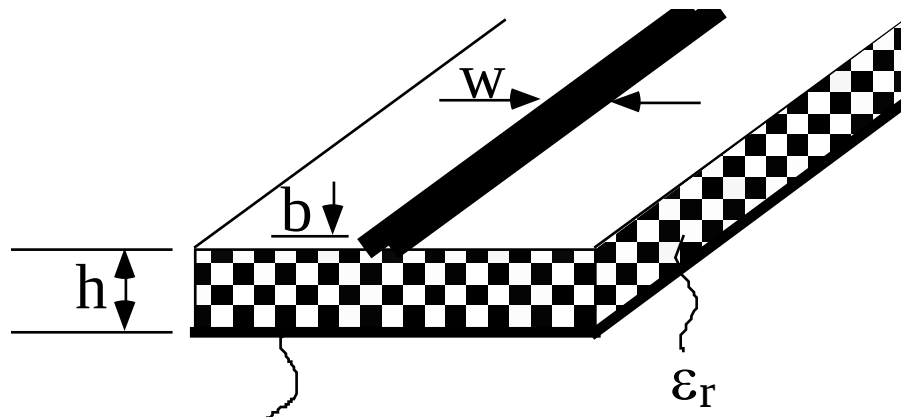
$$\alpha_d = \frac{k \tan \delta}{2} \quad [Np/m]$$

$$\alpha_c = \begin{cases} \frac{0.0027 R_s \epsilon_r Z_c}{30\pi(2h-t)} A & \text{pour } \sqrt{\epsilon_r} Z_c < 120 \\ \frac{0.16 R_s}{Z_c 2h} B & \text{pour } \sqrt{\epsilon_r} Z_c > 120 \end{cases} \quad [Np/m]$$

$$A = 1 + \frac{2w}{2h-t} + \frac{2h+t}{\pi(2h-t)} \ln\left(\frac{4h-t}{t}\right) \quad R_s = \sqrt{\frac{\omega\mu}{2\sigma}}$$

$$B = 1 + \frac{2h}{(0.5w + 0.7t)} \left(0.5 + \frac{0.414t}{w} + \frac{1}{2\pi} \ln \frac{4\pi w}{t} \right)$$

microstrip line



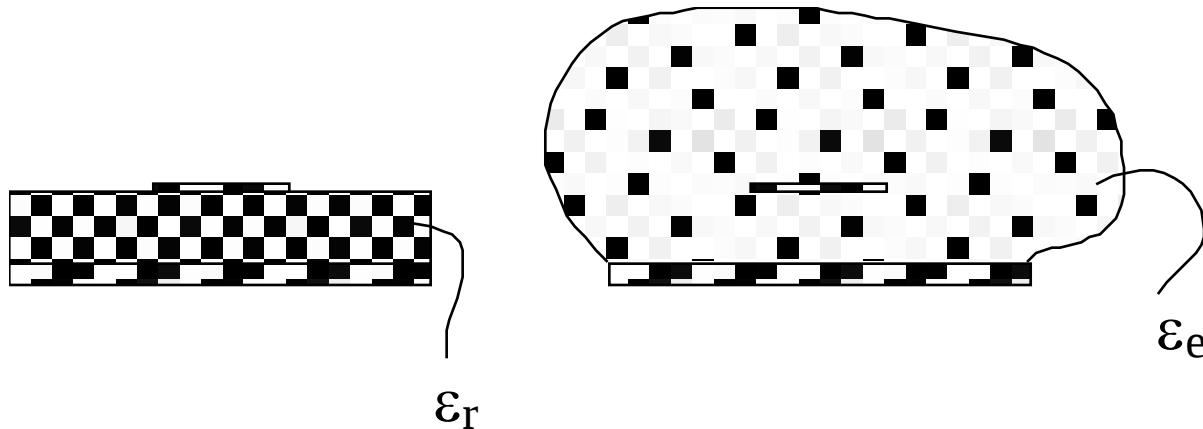
ground plane

microstrip line

- inhomogeneous line, but two conductors (line and ground plane)

Quasi TEM mode

microstrip line : effective permittivity



$$v_{\phi} = \frac{c}{\sqrt{\epsilon_e}}$$

$$\beta = k_0 \sqrt{\epsilon_e}$$

$$1 < \epsilon_e < \epsilon_r$$

microstrip line : effective permittivity

$$\varepsilon_e = \frac{1}{2}(\varepsilon_r + 1) + \frac{1}{2}(\varepsilon_r - 1) \left[\left(1 + 12 \frac{h}{w} \right)^{-0.5} + 0.04 \left(1 - \frac{w}{h} \right)^2 \right] \text{ pour } \frac{w}{h} \leq 1$$

$$\varepsilon_e = \frac{1}{2}(\varepsilon_r + 1) + \frac{1}{2}(\varepsilon_r - 1) \left(1 + 12 \frac{h}{w} \right)^{-0.5} \text{ pour } \frac{w}{h} \geq 1$$

microstrip line : effective permittivity

Error : less than 1 % for

$$0.05 \leq w/h \leq 20 \text{ et } \varepsilon_r \leq 16$$

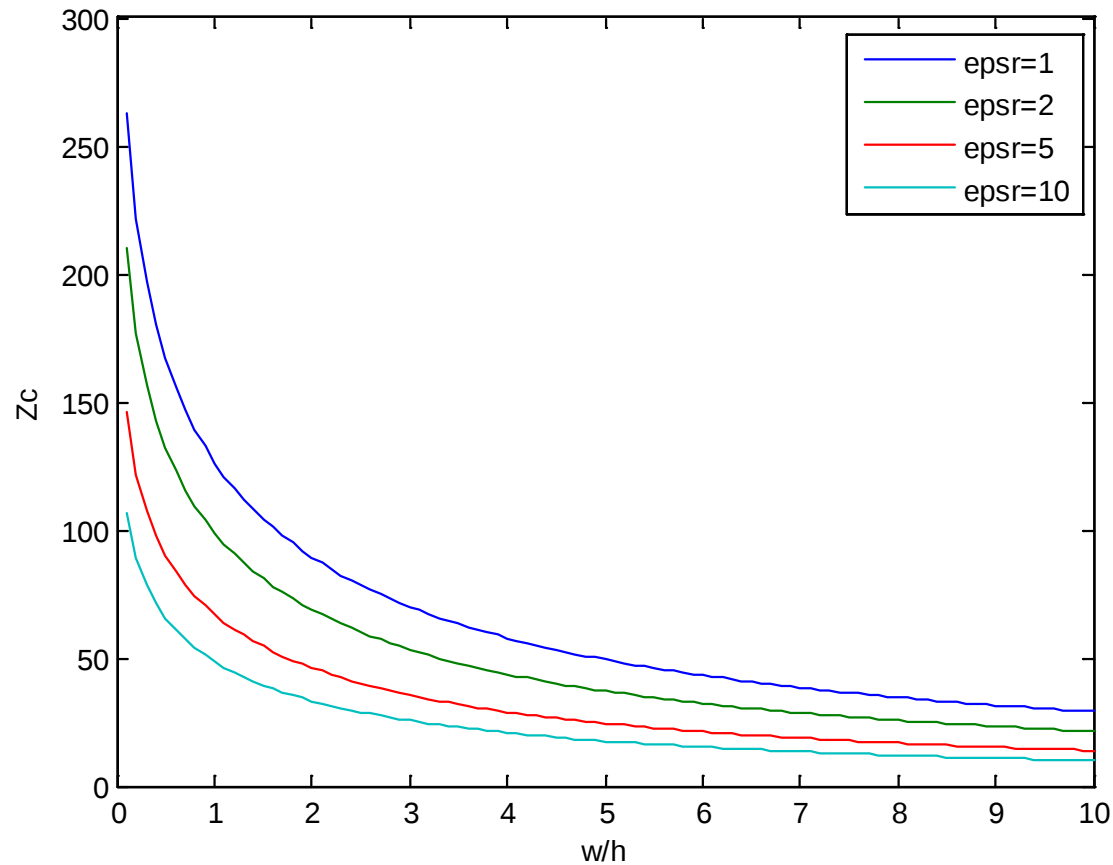
microstrip line : characteristic impedance (analysis)

$$Z_c = \frac{Z_o}{2\pi\sqrt{\epsilon_e}} \ln\left(\frac{8h}{w} + \frac{w}{4h}\right) \quad \text{pour} \quad \frac{w}{h} \leq 1$$

$$Z_c = \frac{Z_o}{\sqrt{\epsilon_e}} \left(\frac{w}{h} + 1.393 + 0.667 \ln\left(\frac{w}{h} + 1.444\right) \right)^{-1} \quad \text{pour} \quad \frac{w}{h} > 1$$

where $Z_o = 120\pi$ is the characteristic impedance of the vacuum

microstrip line : characteristic impedance (analysis)



microstrip line : characteristic impedance (synthesis)

$$\frac{w}{h} = 4 \left[\frac{1}{2} e^A - e^{-A} \right]^{-1} \quad \text{pour} \quad \frac{w}{h} \leq 2$$

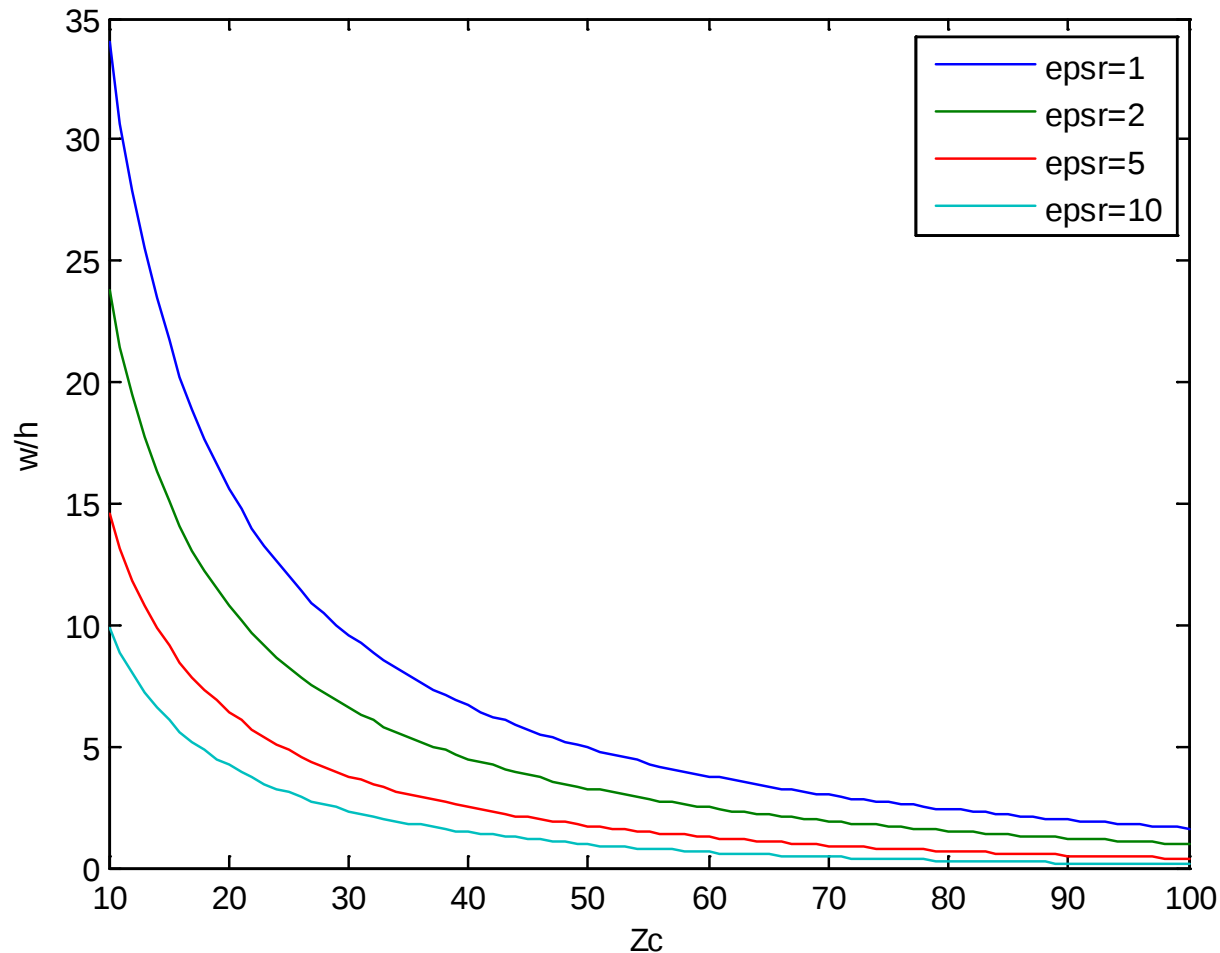
$$\frac{w}{h} = \frac{\epsilon_r - 1}{\pi \epsilon_r} \left(\ln(B - 1) + 0.39 - \frac{0.61}{\epsilon_r} \right) + \frac{2}{\pi} (B - 1 - \ln(2B - 1)) \quad \text{pour} \quad \frac{w}{h} \geq 2$$

with

$$A = \frac{Z_c}{Z_o} \pi \sqrt{2(\epsilon_r + 1)} + \frac{\epsilon_r - 1}{\epsilon_r + 1} \left(0.23 + \frac{0.11}{\epsilon_r} \right)$$

$$B = \frac{\pi}{2\sqrt{\epsilon_r}} \frac{Z_o}{Z_c}$$

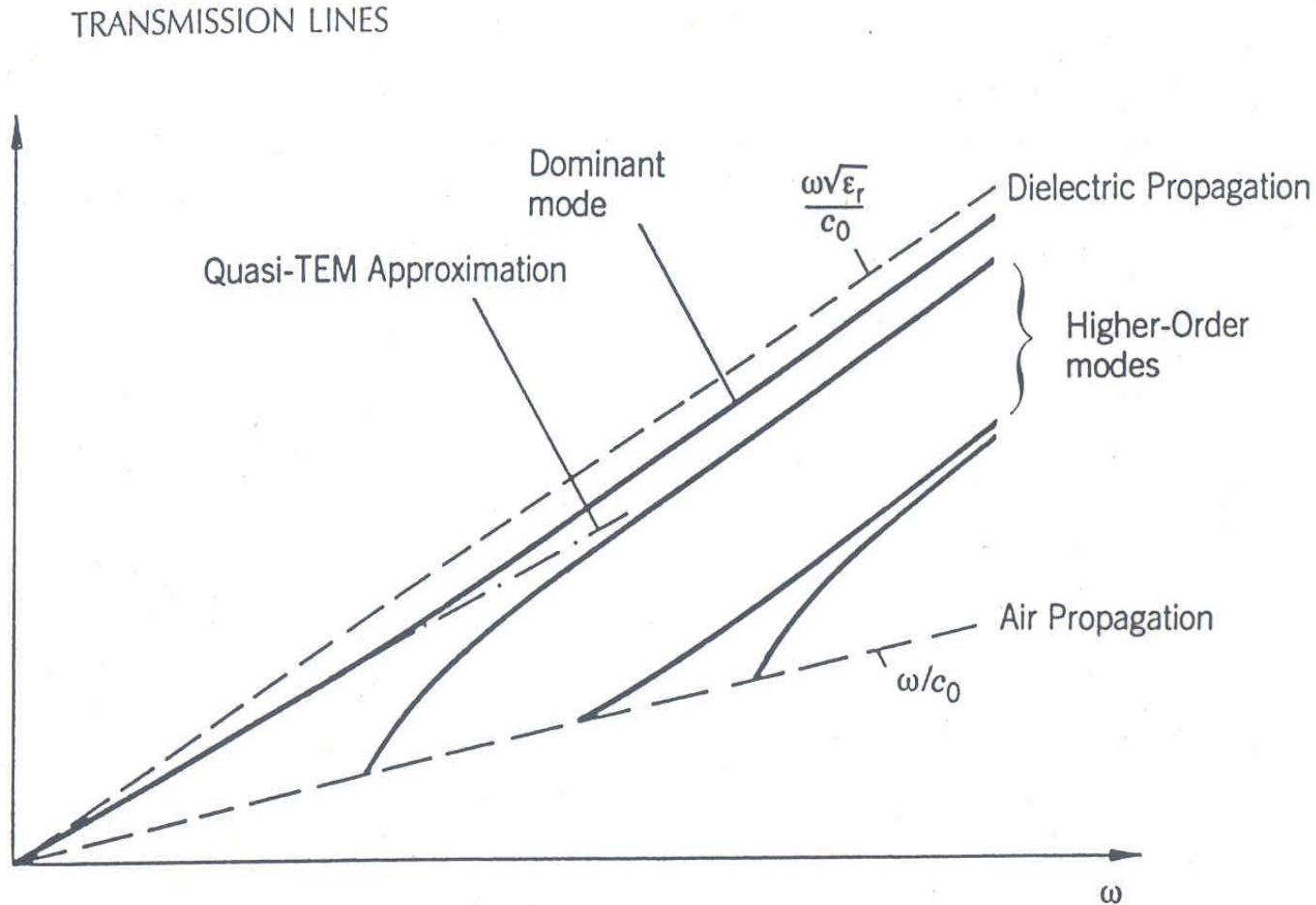
microstrip line : characteristic impedance (synthesis)



Attenuation in a microstrip line

$$\alpha = \alpha_d + \alpha_c \quad [Np / m]$$
$$\alpha_d = \frac{k_o \epsilon_r (\epsilon_e - 1) \tan \delta}{2 \sqrt{\epsilon_e} (\epsilon_r - 1)} \quad [Np / m]$$
$$\alpha_c = \frac{R_s}{w Z_c} \quad [Np / m]$$
$$R_s = \sqrt{\frac{\omega \mu}{2 \sigma}}$$

Modes in a microstrip line



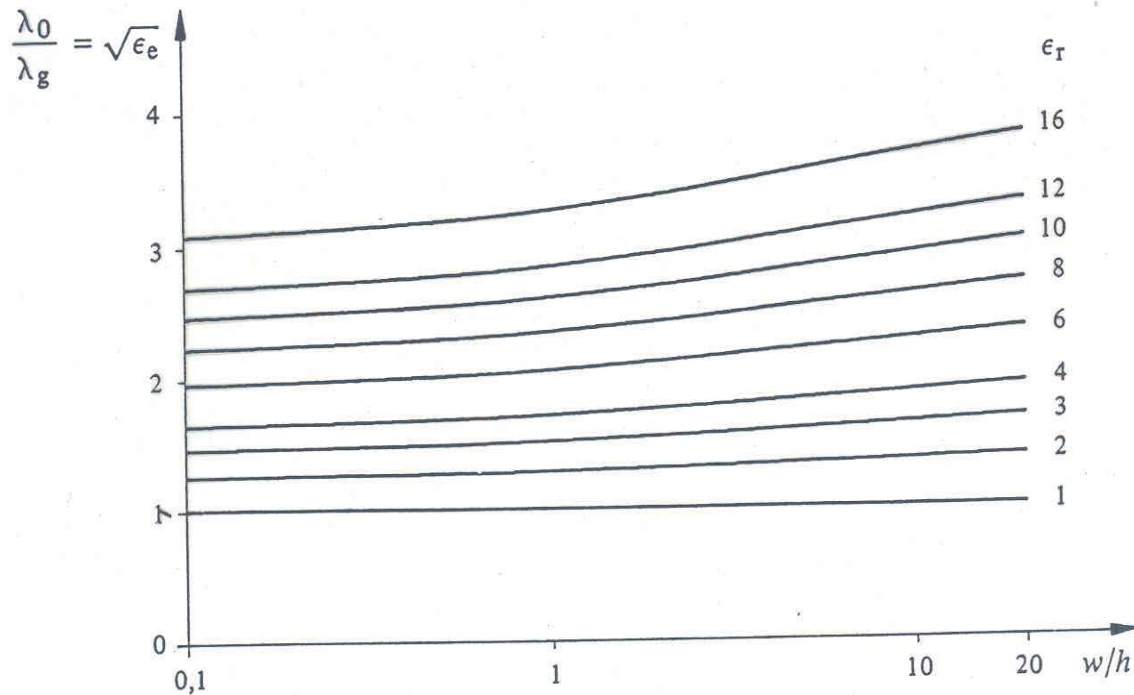
Dispersion in a microstrip line

$$\varepsilon_{\text{ed}}(f) = \varepsilon_r - \frac{\varepsilon_r - \varepsilon_e}{1 + \left(\frac{f}{f_p}\right)^2} G$$

$$f_p = \frac{Z_c}{2h\mu_o}$$

$$G = 0.6 + 0.009Z_c$$

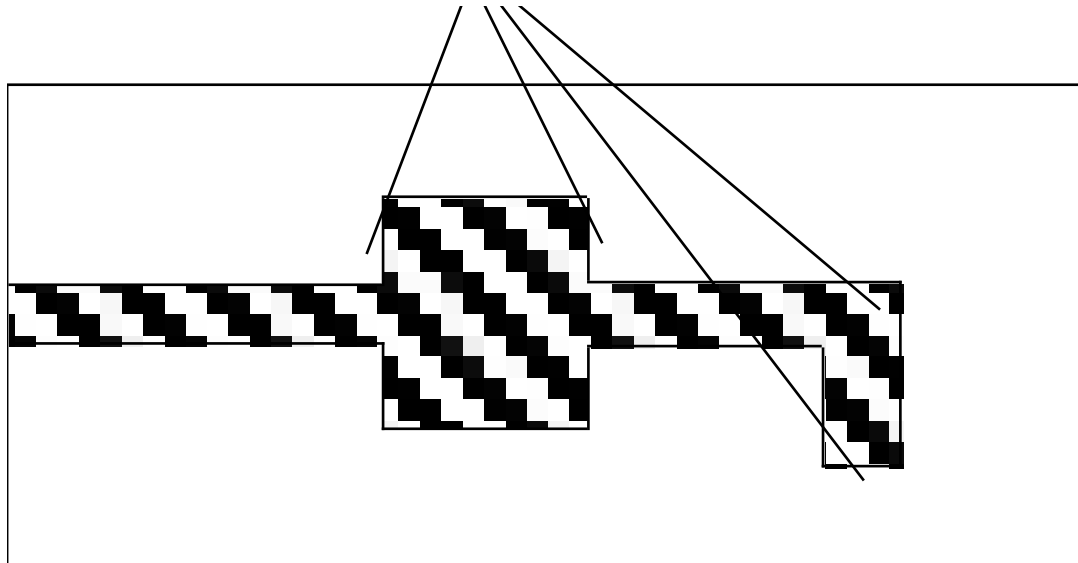
Dispersion in a microstrip line



Radiation of a microstrip line

A TEM mode does not radiate => radiation occurs when higher order modes are excited

Local excitation of higher order modes

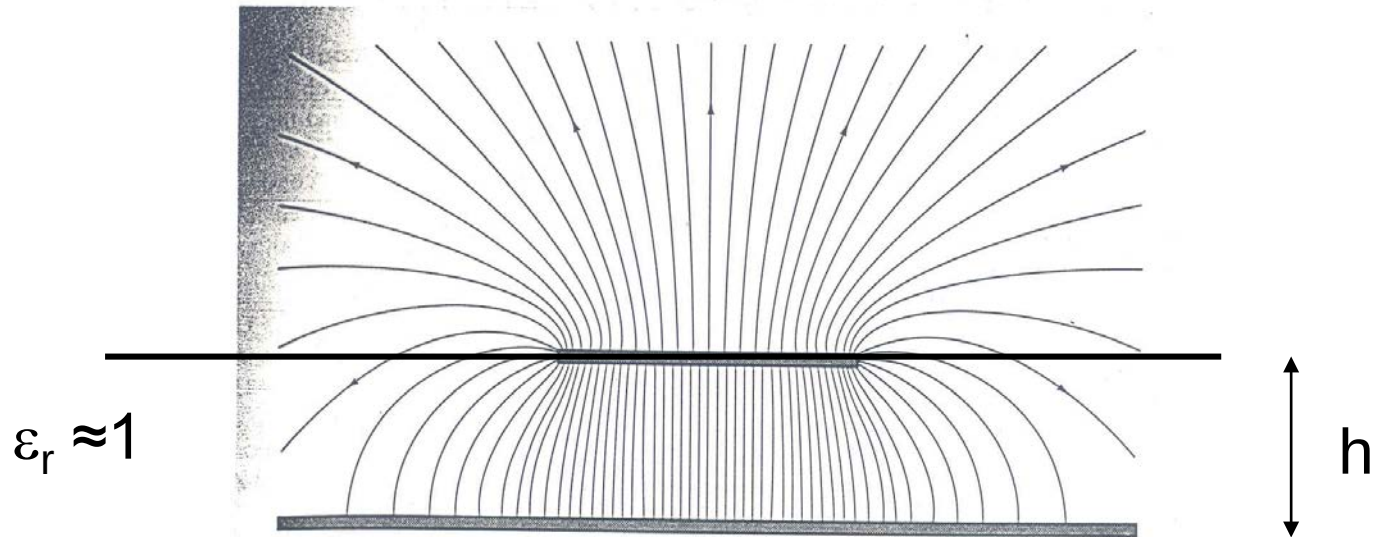


Radiation of a microstrip line

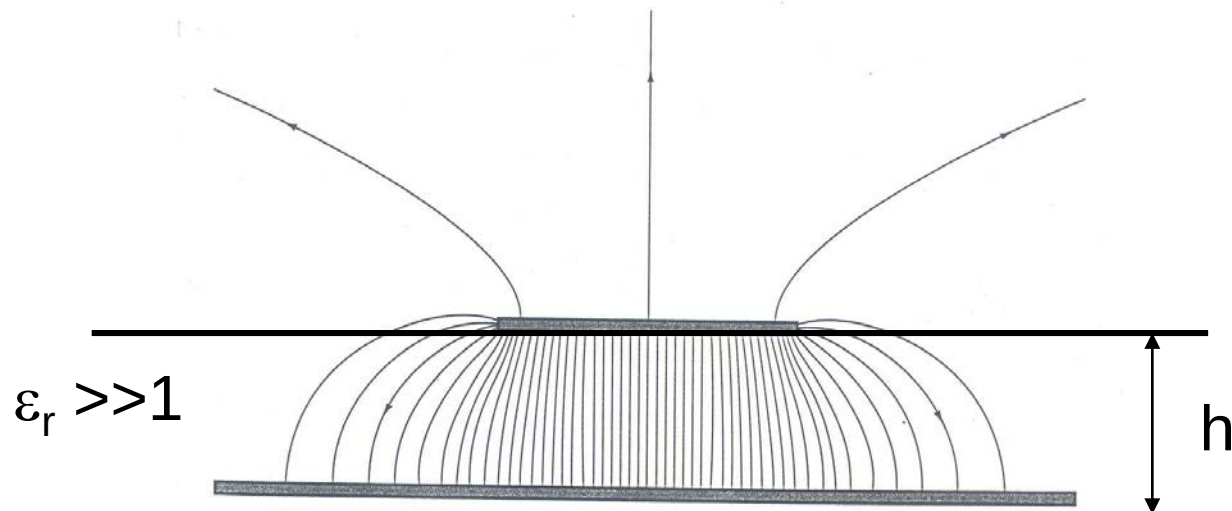
For a $50\ \Omega$ line, the frequency f_m for which the radiated power remains lower than 1 % of the total power is given by :

$$f_m [GHz] = \frac{2.14 \sqrt[4]{\epsilon_r}}{h [mm]}$$

Radiation of a microstrip line



(a)

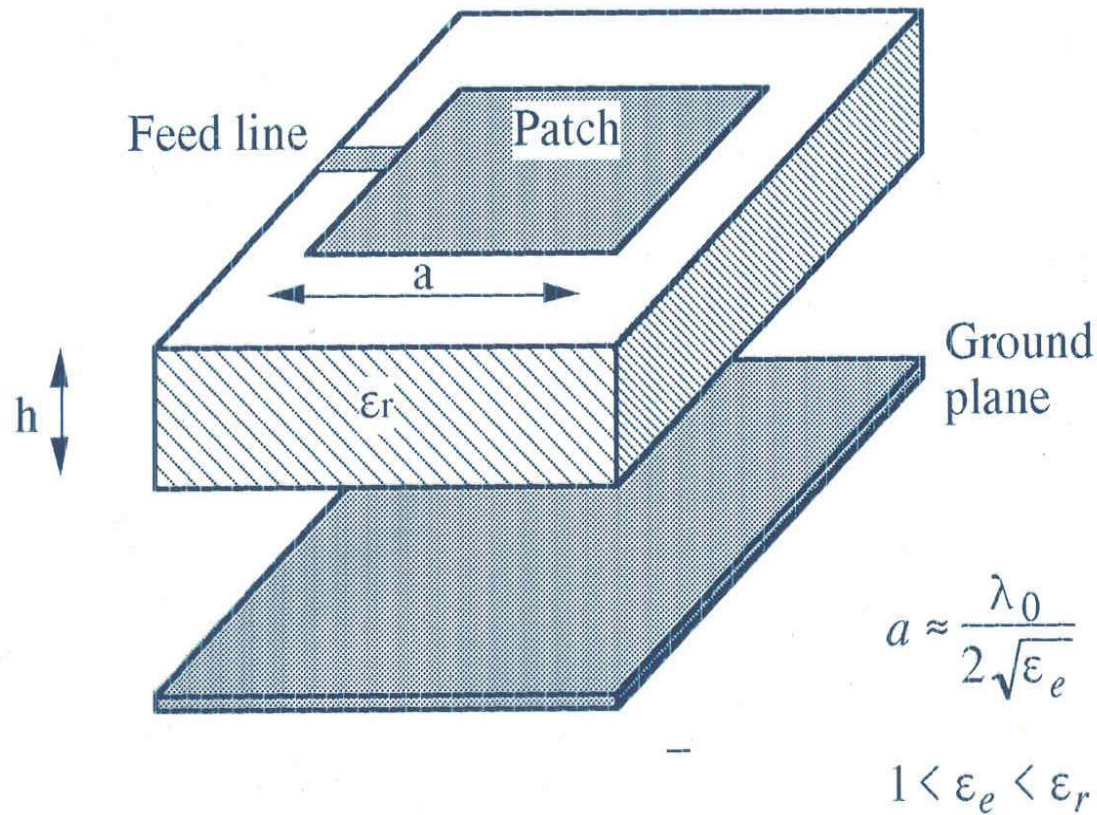


(b)

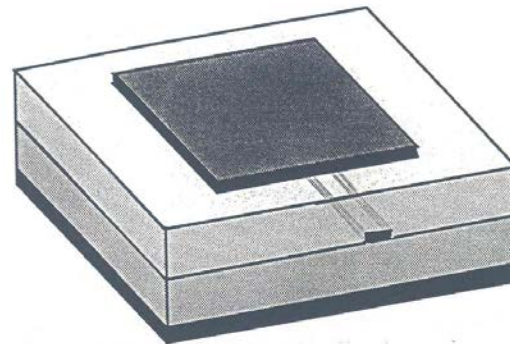
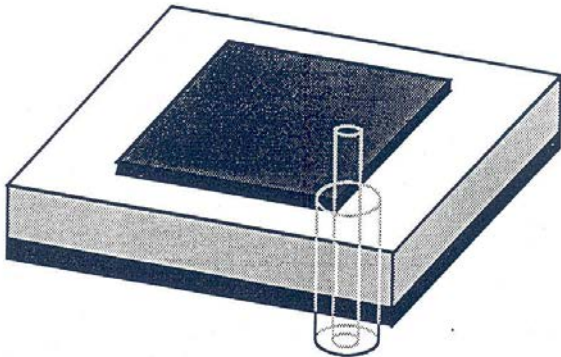
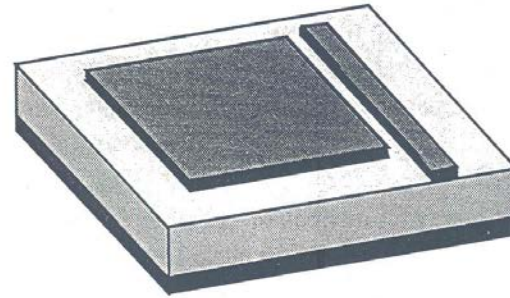
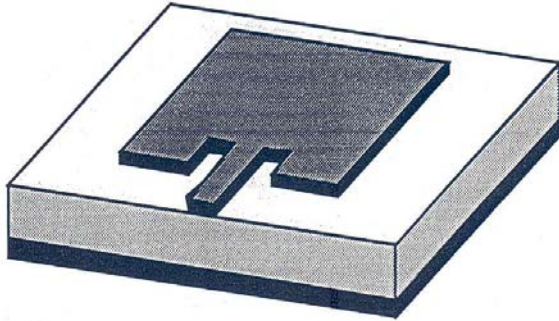
Radiation of a microstrip line

	h/λ_o	ϵ_r
Guided waves	↓	↑
Radiated waves	↑	↓

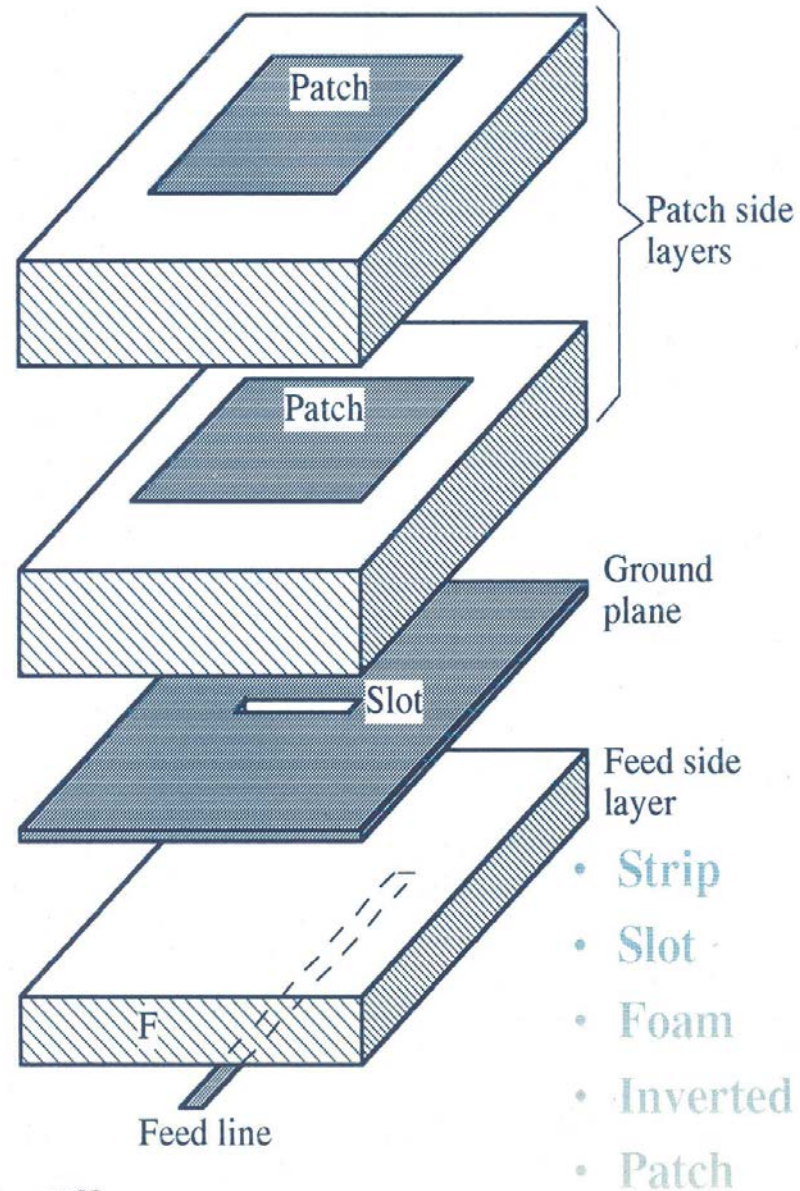
microstrip antenna



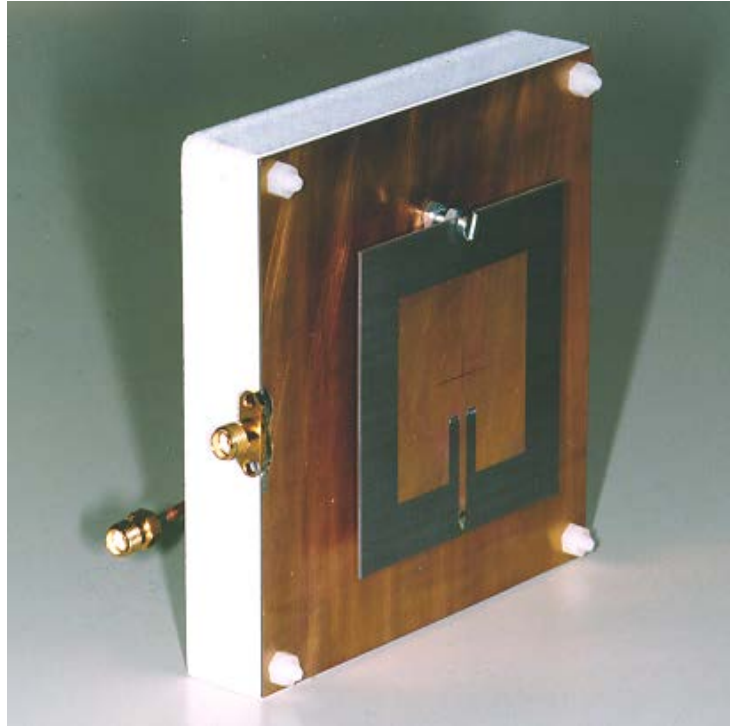
microstrip antenna



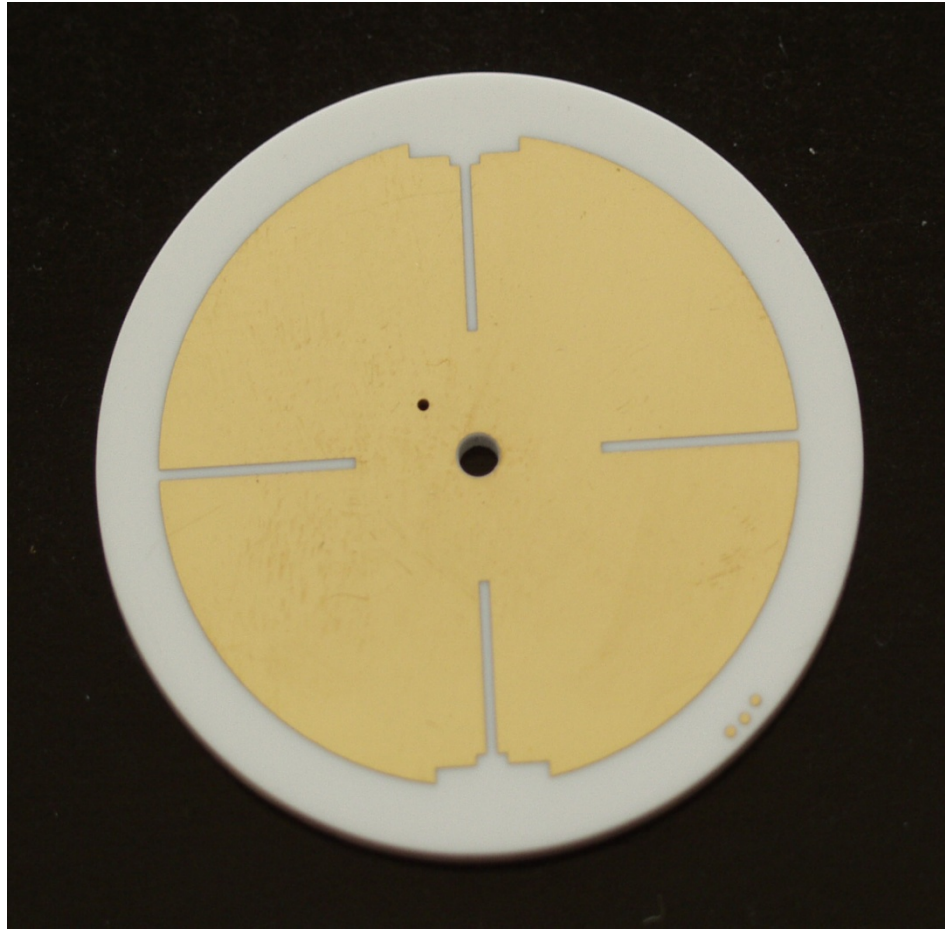
microstrip antenna



Microstrip antenna



Microstrip antenna



	coaxial cable	Waveguide	stripline	microstrip
Dom. mode	TEM	TE ₁₀	TEM	Quasi TEM
other	TE, TM	TE, TM	TE, TM	Hybrid
Dispersion	none	medium	none	low
Bandwidth	high	low	high	high
Lossess	medium	low	high	high
Max Power	medium	high	low	low
Size	big	big	medium	small
Manufactur.	medium	difficult	easy	easy
Component	difficult	difficult	medium	easy